

MGU-UGP (HONOURS)

Syllabus



Mahatma Gandhi University

Kottayam

| Programme | BSc (Hons) Ma | thematics | | | | | |
|-----------------------|--|---|--|--|---|--|--|
| Course Name | Ground Roots of Mathematics | | | | | | |
| Type of Course | DSC A | | | | | | |
| Course Code | MG1DSCMAT | 100 | DHI | | | | |
| Course Level | 100-199 | | | | | | |
| Course Summary | This course pro the principles of plore proposition quantifiers. The basics of funct shifting and sca The core of the are introduced higher derivation metric function tiation. The foo | of calculus onal logic e course t tions and ling, and i e course i to technic wes, produ as using fo cus is on | . Beginnin , propositi hen transit their grap ntroducing s dedicated ques of dif ct and que ormulas, th practical a | g with "Basi ional equiva- tions to "Fun- ohs, combini- g inverse fund d to "Deriva ferentiation otient rules, o e chain rule, | c Logic" lence, pr nctions", ing funct ctions. tives", w without t derivative and imp | , students ex- edicates, and covering the ions through here students formal proof, es of trigono- licit differen- | |
| | real-world problem-solving. The course concludes with an exploration of the "Applications of De- rivatives", emphasizing the analysis of functions. Topics include de- termining intervals of increase, decrease, and concavity, identifying relative extrema with geometric implications of multiplicity, applying L'Hôpital's Rule, and addressing indeterminate forms. | | | | | | |
| Semester | 1 | Credits | Tutorial | Droationer | Others | 4 | |
| Course Details | Learning Approach | Lecture 3 | Tutorial 0 | Practicum 1 | Others 0 | Total Hours 75 | |

| Pre- requisites, If any | Sets, Set operations and Limits |
|----------------------------|---------------------------------|
| II ully | Sets, Set operations and Emilia |

| CO No: | Expected Course Outcome | Learning Domains | PO No: | | | |
|--|---|---------------------|------------------|--|--|--|
| | Upon the successful completion of the course, the student will be able to | | | | | |
| 1 | Understand the language of Mathematics and communicate in a proper way. | U | 1, 2, 3, 4, 10 | | | |
| 2 | Understand the geometry of basic functions and their properties. | U | 1, 2, 3, 10 | | | |
| 3 | Analyse the conditions for a function to have an inverse. | An | 1, 2, 3 | | | |
| 4 | Understand and apply the process of differentiation. | А | 1, 2, 3, 10 | | | |
| 5 | Characterize increasing/decreasing functions using their derivatives. | U | 1, 2, 3, 10 | | | |
| 6 | Apply L'Hôpital's rule to evaluate indeterminate forms. | А | 1, 2 | | | |
| 7 | Experience graphing tools in doing and enjoying Mathematics | S | 1, 2, 3, 4, 9,10 | | | |
| *Remember (K), Understand (U), Apply (A), Analyse (An), Evaluate (E), Create (C), Skill (S), Interest (I) and Appreciation (Ap) | | | | | | |

COURSE OUTCOMES (CO)



Content for Classroom transaction (Units)

| Module | Units | Course Description | CO No: | Hours |
|--------|-------|----------------------------|--------|-------|
| 1 | | Basic Logic | | |
| | 1.1 | Propositional Logic | 1 | |
| | 1.2 | Propositional Equivalence | 1 | 15 |
| | 1.3 | Predicates and Quantifiers | 1 | |
| | | Problems (Practicum) | 1 | |

| | Text 2 | : Chapter 1- Sections: 1.1, 1.3, 1.4 | | |
|---|--------|---|----------------|----|
| 2 | | Functions | | |
| | 2.1 | Set, Set operations, Set identities (Review) | 1 | |
| | 2.2 | Functions and their graphs (excluding representing functions numerically) | 2 | |
| | 2.3 | Combining Functions: Shifting and scaling Graphs | 2,7 | 20 |
| | 2.4 | Inverse Functions | 3 | |
| | | Problems (Practicum) | 1, 2, 3, 7 | - |
| | | : Chapter 1 - Sections: 1.1, 1.2, Chapter 7 - Section ons only) | n: 7.1 (Invers | e |
| 3 | | Derivatives | | |
| | 3.1 | Introduction to Techniques of Differentiation (without proof) | 4 | |
| | 3.2 | Higher derivatives, The product and quotient rules | 4 | |
| | 3.3 | Derivatives of trigonometric functions (Using formulas only) | 4 | 20 |
| | 3.4 | Chain Rule | 4 | |
| | 3.5 | Implicit Differentiation | 4 | |
| | | Problems (Practicum) | 4 | |
| | Text 1 | : Chapter 2 - Sections: 2.3 to 2.7 | | |
| 4 | | Applications of derivatives | | |
| | 4.1 | Analysis of Functions I: Increase, decrease and concavity | 5,7 | |
| | 4.2 | Analysis of Functions II: Relative extrema | 5,7 | 1 |
| | 4.3 | L'Hôpital's Rule | 6 | 20 |
| | 4.4 | Indeterminate forms | 6 | |
| | | Problems (Practicum) | 5, 6, 7 | |

| | Text 1: Chapter 3 - Sections: 3.1, 3.2 (Geometric implications of multiplicity, Analysis of polynomials excluded), Chapter 6 - Section:6.5 |
|---|---|
| | Teacher Specific Contents |
| | (This can be either classroom teaching, practical session, field visit etc. as |
| 5 | specified by the teacher concerned) |
| | This content will be evaluated internally |
| | |

Practicum

Practicum is designed to provide supervised practical application of theoretical knowledge and skills.

It's purpose is to encourage creativity and develop Problem Solving Skills.

The practicum component is to be done in the classroom under the strict guidance of the teachers.

A minimum of 30 problems is to be solved, and a handwritten copy of the solutions should be kept in the department.

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| Teaching and Learning Approach | Lecture, Tutorial and Activity oriented | | | | | |
|--------------------------------------|--|--------------------|-------------------|--|--|--|
| - | MODE OF ASSESSMENT | | | | | |
| | A Continuous Comprehensive Assessment (CCA) 30 Marks | | | | | |
| | _ | Components | Mark Distribution | | | |
| | _ | Module Test- I | 5 Marks | | | |
| | _ | Module Test- II | 5 Marks | | | |
| Assessment | _ | Module Test- III | 5 Marks | | | |
| Types | - | Module Test- IV | 5 Marks | | | |
| | - | Assignment/Seminar | 5 Marks | | | |
| | | Quiz/Viva voce | 5 Marks | | | |

| В | End Semester Evaluation (ESE) 70 marks | | | | | |
|---|--|-------------|-------------|-------------|-------------|--|
| | Question Pattern | | | | | |
| | [Maximur | n Time 2 Ho | ours, Maxim | um Marks 70 |] | |
| | | Part A | Part B | Part C | T (1 | |
| | Module | 2 Marks | 6 Marks | 10 Marks | Total | |
| | Ι | 2 | 2 | 1 | 5 | |
| | II | 2 | 2 | 2 | 6 | |
| | III | 2 | 2 | 1 | 5 | |
| | IV | 2 | 2 | 2 | 6 | |
| | Total no of questions | D 8 | 8 | 6 | 22 | |
| | Number of questions to be answered | 5 | 5 | 3 | 13 | |
| | Total Marks | 10 | 30 | 30 | 70 | |

REFERENCES:

- Anton, Howard, Irl Bivens, Stephen Davis. *Calculus*. 10th ed. John Wiley & Sons, Inc., 2012.
- 2. Rosen, Kenneth H. *Discrete Mathematics and Its Applications* (7th ed.). McGraw Hill Publishing Co. New Delhi, 2013. **(HONOURS)**
- 3. Thomas, George B., Jr., and Maurice D. Weir. *Thomas' Calculus*. 12th ed. Pearson, 2009.

Syllabus

SUGGESTED READINGS:

- Hofstadter, Douglas R. *Gödel, Escher, Bach: An Eternal Golden Braid*. Expanded ed. Basic Books, 2007.
- 2. Copi, Irving M., Carl Cohen. Introduction to Logic. 5th ed. Routledge, 2018.
- 3. Stewart, James. Calculus: Early Transcendentals. 10th ed. Cengage Learning, 2023.
- 4. Thompson, Silvanus P. Calculus Made Easy. 5th ed. Dover Publications, 2014.
- Thomas, George B., Jr., and Maurice D. Weir. *Thomas' Calculus*. 15th ed. Pearson, 2023.

ADVANCED READINGS:

- 1. Hurley, Patrick J. *A Concise Introduction to Logic*. 11th ed. Wadsworth Publishing, 2018.
- 2. Copi, Irving M., Carl Cohen. *Symbolic Logic*. 13th ed. W.W. Norton & Company, 2019.
- 3. Davis, Philip J. Advanced Calculus. 7th ed. Wiley-Interscience, 2002.
- 4. Tu, Loring W. Introduction to Manifolds. 3rd ed. Springer, 2012.

SOME SUGGESTIONS FOR TEACHER SPECIFIC CONTENTS:

- ➤ Determine the output of a combinatorial circuit constructed using basic logic gates. Also Build a digital circuit produces the required output. (Eg: Build a digital circuit that produces the output $(p \lor \neg r) \land (\neg p \lor (q \lor \neg r))$ with input bits p, q and r.
- > Determine whether a given function is injective or surjective using horizontal line test.
- Using a graphing calculator, visualize the effect of stretching and scaling (horizontal &vertical) of functions.
- Using a graphing calculator, plot the inverse of graphs and understand the geometric relationship between a graph and its inverse.
- Match the graphs of functions with the graphs of their derivatives. (Eg: Question 23 of section 2.2 in text 3).
- Use a graphing utility to make rough estimates of the locations of all horizontal tangent lines (Eg: Question 49 & 50 of section 2.3 in text 3).
- > Use a graphing utility to make rough estimates of the intervals on which fr(x) > 0 (Eg: Questions 63 & 64 of section 2.3 in text 3).
- Use the implicit plotting capability of a CAS to graph a curve. (Eg: Question 45 of section 2.7 in text 3), Suggested software: Desmos, GeoGebra etc.



Mahatma Gandhi University

Kottayam

| Programme | | | | | | |
|----------------------------|---|----------|-------------|-----------|-------------|----------------|
| Course Name | Mathematics | for Comp | etitive Exa | minations | | |
| Type of Course | MDC | GA | NDH | | | |
| Course Code | MG1MDCMAT100 | | | | | |
| Course Level | 100-199 | | | | | |
| Course Summary | This competitive exam-focused mathematics course covers crucial top- ics like number systems, logical reasoning, data analysis, and mathe- matical measurements. This course explores concepts such as HCF, LCM, fractions, ratio, percentage, and time-related problem-solving, providing comprehensive preparation for various competitive examina- tions. | | | | | |
| Semester | 11GU Credits (HONOURS) 3 | | | | | |
| Course Details | Learning Approach | Lecture | Tutorial | Practicum | Others 0 | Total Hours 60 |
| Pre- requisites, If any | | ₩ £ ↓ | | . ~ | | |

COURSE OUTCOMES (CO)

| CO No: | Expected Course Outcome | Learning Domains | PO No: |
|--------|---|---------------------|----------|
| | Upon the successful completion of the course, the student will be able to | | |
| 1 | Develop a solid understanding of various types of | K, U, E | 1, 2, 10 |

| | numbers. Master techniques for calculating HCF | | |
|--------|---|---------|----------------|
| | and LCM and gain proficiency in simplifications, | | |
| | squares and square roots. | | |
| | Acquire logical reasoning skills by exploring | | |
| | concepts such as ratio, proportion, percentage, and | | |
| 2 | solving problems related to profit, loss and age | K, U, E | 1,2, 3, 4, 10 |
| | and apply these principles to real world scenarios. | | |
| | Learn the essentials of data analysis, including | | |
| | concepts of simple interest, compound interest and | K, U, A | 1, 2, 3, 10 |
| 3 | solving calendar problems. Develop analytical | | |
| | skills to interpret and utilize data effectively. | | |
| | Gain expertise in mathematical measurements | | |
| | through topics like time and work, time and | | |
| 4 | distance, and stocks and shares. Apply | K, A, E | 1, 2, 3, 10 |
| | mathematical concepts to solve practical problems | | |
| | in these areas. | | |
| *Remen | nber (K), Understand (U), Apply (A), Analyse (An), Skill (S) Interest (I) and Appreciation | |), Create (C), |

Skill (S), Interest (I) and Appreciation (Ap)

ावद्यथा असूतसञ्चत्रत

COURSE CONTENT

Content for Classroom transaction (Units)

| Module | Units | Course Description | CO No: | Hours |
|--------|---------|---|--------|-------|
| 1 | | Number System and Numerical Techniques | | |
| | 1.1 | Type of Numbers | 1 | |
| | 1.2 | HCF and LCM of Numbers | 1 | 18 |
| | 1.3 | Decimal Fractions, Simplification | 1 | |
| | 1.4 | Square Roots and Cube Roots | 1 | |
| | | Problems (Practicum) | 1 | |
| | Text 1: | Relevant Portions | · · · | |

| 2 | | Logical Reasoning & Data Analysis | | | |
|---|--|-------------------------------------|------|----|--|
| | 2.1 | Ratio and Proportion | 2 | | |
| | 2.2 | Percentage | 2 | | |
| | 2.3 | Profit and Loss | 2 | | |
| | 2.4 | Problems on Ages | 2 | 24 | |
| | 2.5 | Simple Interest & Compound Interest | 3 | | |
| | 2.6 | Calendar | 3 | | |
| | | Problems (Practicum) | 2, 3 | | |
| | Text 1: | Relevant Portions | | | |
| 3 | | Mathematical Measurements | | | |
| | 3.1 | Time and Work | 4 | 18 | |
| | 3.2 | Time and Distance | 4 | | |
| | 3.3 | Stocks and Shares | 4 | | |
| | | Problems (Practicum) | 4 | | |
| | Text 1: Relevant Portions | | | | |
| 4 | MOU Teacher Specific Contents | | | | |
| | (This can be either classroom teaching, practical session, field visit etc. as | | | | |
| | specified by the teacher concerned) | | | | |
| | This content will be evaluated internally | | | | |

Practicum

Practicum is designed to provide supervised practical application of theoretical knowledge and skills.

It's purpose is to encourage creativity and develop Problem solving skills.

The practicum component is to be done in the classroom under the strict guidance of the teachers.

A minimum of 30 problems is to be solved, and a handwritten copy of the solutions should be kept in the department.

| Teaching and Learn- ing Ap- proach | Classroom Procedure (Mode of transaction) | | | | |
|---|---|--|-------------------|--|--|
| | Lecture and Tutorial | | | | |
| | MODE OF ASSESSMENT | | | | |
| Assessment Types | A | Continuous Comprehensive Assessment (CCA) 25 Mark | | | |
| | | Components | Mark Distribution | | |
| | | Module Test- I | 5 Marks | | |
| | | Module Test- II | 5 Marks | | |
| | | Module Test- III | 5 Marks | | |
| | | Assignment/Seminar | 5 marks | | |
| | | Quiz/Viva voce | 5 Marks | | |
| | В | End Semester Evaluation (ESE) 50 marks | | | |
| | | (MCQ Examination) | | | |
| | | [Maximum Time 75 Minutes, Maximum Marks 50] | | | |
| | | Module Number of Questions | | | |
| | | I 8 | | | |
| | | II 14 | | | |
| | | III 2 1 1 1 1 2 8 | | | |
| | | Answer any 25 questions out of 30 Multiple Choice Questions. Each question carries 2 marks. | | | |

REFERENCES:

1. Aggarwal, R.S. *Quantitative Aptitude,* Sultan Chand and company Ltd, New Delhi, 2017. **SUGGESTED READINGS:**

- 1. Abhijit Guha, *Quantitative Aptitude for Competitive Examinations*, McGraw Hill Education 2011.
- 2. Tyra M., Magical Book on Quicker Maths., BSC Publishing Company, 2018.

SOME SUGGESTIONS FOR TEACHER SPECIFIC CONTENTS:

- Discuss different number systems, such as decimal, binary, octal, and hexadecimal, and their conversions.
- Show how number theory concepts apply in various real-life scenarios, like cryptography or data encoding.
- Provide examples where LCM and HCF are used, such as in simplifying fractions, adding and subtracting fractions, or solving equations.
- Incorporate problems where knowledge of roots is essential, such as in Geometry, Physics, or Engineering.
- Provide examples where ratios and proportions are used in real-life situations, such as in finance, cooking, or map scales.
- Provide examples of profit and loss situations in business, trading, and investment scenarios.
- Discuss problem-solving strategies for analyzing profit and loss situations and determining the best course of action.
- Provide examples of interest calculations in banking, investments, loans, and savings accounts.
 MGU-UGP (HONOURS)
- Show the difference between simple interest and compound interest and how they affect the total amount over time.
- Provide examples of time and work problems in production scenarios, team projects, or construction projects.